



Testing and validating an uncertainty budget

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fiducial reference measurements for satellite ocean colour





Metrology for Earth Observation and Climate http://www.emceoc.org



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Recap: Calculating the measurement uncertainty



$$u_{c}^{2}(y) = \sum_{i=1}^{n} \left(\frac{\partial f}{\partial x_{i}}\right)^{2} u^{2}(x_{i}) + 2\sum_{i=1}^{n-1} \sum_{j=i+1}^{n} \frac{\partial f}{\partial x_{i}} \frac{\partial f}{\partial x_{j}} u(x_{i}, x_{j})$$

Need to know / work out:

- What affects the measurement result?
- How big is the uncertainty associated with each of these effects?
- How sensitive is the result to each of these effects?
- Are effects correlated?

We have the answer!



- "Plug everything into the equation"
- And we have our uncertainty!

$$u_{c}^{2}(y) = \sum_{i=1}^{n} \left(\frac{\partial f}{\partial x_{i}}\right)^{2} u^{2}(x_{i}) + 2\sum_{i=1}^{n-1} \sum_{j=i+1}^{n} \frac{\partial f}{\partial x_{i}} \frac{\partial f}{\partial x_{j}} u(x_{i}, x_{j})$$

Or do we?

How do we know we've got the 'right' uncertainty?

Testing and validating an uncertainty budget



- Make a new experiment to achieve the same end point
- Change as much as possible between the two experiments
- Work out new uncertainty budget
- Do they agree within uncertainties?

Testing and validating an uncertainty budget



- Repeat the measurement on another occasion; vary as much as possible
 - Use different reference(s)
 - Use different instrument(s)
 - Get someone else to do the measurement
 - Change the order of the measurements
- Use a different measurement method e.g.
 - Calibration directly against another radiance gauge rather than lamptile combination
 - Array spectrometer or scanning instrument
- Compare with someone else
 - Compare results, uncertainties and uncertainty budgets
 - Helps quantify 'known unknowns'
 - Helps identify 'unknown unknowns'

Testing and validating an uncertainty budget



possible

- Repeat the measurement on another occ
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 - Use a range of artefacts Use different instrument(s
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Comparing methods

Optical method – scan laser beam over surface





Source of Uncertainty	Value (µm)	Value/√3 (µm)
Interferometer drift	± 0.02	±0.012
Inteferometer alignment	$\pm 0.03 (5 \text{ mm } \phi)$	±0.017
	$\pm 0.12 \ (20 \ mm \phi)$	±0.069
	±0.15 (25 mm φ)	±0.087
Laser stability	±0.04	±0.023
Environmental conditions	**	**
Resolution	±0.06	±0.035
Combined uncertainty		
Nominal 5 mm ø	± 0.11	±0.05
Nominal 20 mm ø	±0.16	±0.08
Nominal 25 mm ø	±0.19	± 0.10

Comparing methods

Contact method – CMM: mechanically scan ball-ended stylus over surface





Source	μm	ppm
Machine scale uncertainty	0.04	
Temperature difference in beam paths during calibration		0.01
Laser frequency difference		0.02
Measurement Reproducibility	0.04	0.04
Edlen Equation		0.03
Index of Refraction-Air Temperature		0.01
Index of Refraction –Air Pressure		0.04
Index of Refraction – Humidity		0.03
Thermal Expansion		0.05
Coefficient of Thermal Expansion		0.05
Contact Deformation	0.002	
Gage Surface Geometry	0.004	
Gage Form Estimation Technique	0.005-0.100	
$U (um) = 0.11 \ \mu m + 0.20 \times 10^{-6} L \ (k=2) \ best$		



$$E_N = \frac{|E_1 - E_2|}{\sqrt{U_1^2 + U_2^2}}$$

E is measurement result *U* is associated expanded uncertainty

 $E_N < 1.0$ indicates results agree with each other within the limits expected based on their associated uncertainties







 $E_N = 0.4$

Results agree to well within uncertainties⇒ Uncertainties (probably) correctly evaluated





Results differ by much more than uncertainties ⇒ Uncertainties underestimated and/or some contributions missing



Comparing with another lab











- Within lab agreement (using different methods)
 mixed results
 - Significant differences between labs
 - Suggests underestimated uncertainties and/or unidentified errors









0.050%

Error bars k = 1

LNETINM

- Within lab agreement (using different methods) mixed results
 - Even larger differences between labs
- Suggests underestimated uncertainties and/or unidentified errors
- Difference (Lab-RV) [%] Suggests properties of aperture being measured are critical



Conclusions





- Even where a lab had good agreement internally between different methods, agreement with other labs was not good
- Uncertainties underestimated by most labs
- Using a range of artefacts revealed additional differences and helped understand measurements better

Example 2: Electrical power of LED lighting products





Example 2: Electrical power of LED lighting products





- All results are in agreement
- Large variation in claimed uncertainties

Example 2: Electrical power of LED lighting products





- Only a few results are in agreement
- Large variation in claimed uncertainties
- Many uncertainties appear to be underestimated

Example 2: Electrical power of LED lighting products

- Uncertainties appear 'correct' for one lamp, but generally underestimated for the other
- Using a range of artefacts
 helps understand
 measurements better
- Errors would not have been known without comparison



Participants

Centre for

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International system for assuring quality of results





International system for assuring quality of results



'Rules' have been established by NMIs for conducting and analysing comparisons



Luminous intensity

Agreed rules for NMI comparisons



- Must define artefacts and set up to be used in advance ('technical protocol')
 - Minimise additional uncertainties due to comparison itself Use more than one artefact type if possible
- Participants use own traceability routes and methods Reveal differences due to these effects
- Participants provide detailed uncertainty budgets
 Allows sharing of ideas and methods
- Blind comparison
 Ensures reliability and integrity of comparison results
- Agree in advance how to present results e.g. what is comparison reference value Avoids debates on how to do this!

Framework for assuring quality of EO data







- The Quality Assurance for Earth Observation (QA4EO) framework
- Looks to make the GUM accessible to the EO community

Community-specific guidelines cannot be

Identifier	Identifier Description	
않 상 'All da	QA4EO Principle: ta and derived products shall have associated wit a fully traceable indicator of their quality'	h them
QA4EO-WGCV-IVO- CLP-004	A best practice guide to land "test-site" characterisation	
QA4EO-WGCV-WO- CUP-005	Guidelines for the identification and set-up of new systems complying with requirements for satellite ocean color applications	
QA4EO-WGCV-MO- CLP-006	Methodologies that should be applied to determine immersion factors for both radiance and irradiance underwater sensors	
QA4EO-WGCV-WO- CLP-007	Absolute Calibration using Rayleigh Scattering	NPL
QA4EO-WGCV-WO- CLP-008	Protocol for the CEOS WGCV pliot Comparison of techniques/Instnuments used for vicarious calibration of land surface imaging through a ground reference standard test site	Training

Framework for assuring quality of EO data





The QA4EO PRINCIPLES provides the background to QA4EO and introduces the key guidelines:

QA4EO-QAEO-GEN-DQK-001	A guide to establish a Quality Indicator on a satellite sensor derived data product
QA4EO-QAEO-GEN-DQK-002	A guide to content of a documentary procedure to meet the Quality Assurance requirements of CEOS
QA4EO QAEO-GEN-DQK-003	A guide to "reference standards" in support of Quality Assurance requirements of QA4EO
QA4EO-QAEO-GEN-DQK-004	A guide to comparisons – organisation, operation and analysis to establish measurement equivalence to underpin the Quality Assurance requirements of QA4EO
QA4EO-QAEO-GEN-DQK-005	A guide to establishing validated models, algorithms and software to underpin the Quality Assurance requirements of QA4EO
QA4EO-QAEO-GEN-DQK-006	A guide to expression of uncertainty of measurements
QA4EO-QAEO-GEN-DQK-007	A guide to establishing quantitative evidence of traceability to underpin the Quality Assurance requirements of QA4EO

Guidelines are based on NMI 'rules' for conducting and analysing comparisons

FRM4SOC LCE-1



 Purpose is to verify the performance of reference irradiance sources used in calibration of Ocean Colour Radiometers

All are FEL-type, but several different manufacturers

- Participants use own traceability routes; all traceable to SI Confirm consistency between these routes
- Lamps have been used for varying amounts of time since calibration

Allow for up to 50 hours ageing in uncertainty budget for comparison

Analysis of FRM4SOC LCE-1



- Want to confirm consistency of traceability routes, not to establish a single reference scale for all calibrations
 Will compare each individual lamp to the mean of all lamps
- Uncertainty associated with each lamp will be combination of:
 - Assigned calibration uncertainty (from certificate)
 - Uncertainty allowance for up to 50 hours ageing
 - Measurement uncertainties associated with the comparison at NPL (e.g. system noise and stability, lamp current, lamp alignment, distance setting)
- Results will be consistent if all lamps agree with mean value to within the associated uncertainties

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Analysis of FRM4SOC LCE-1





Things to take away from this module



- It's important to test / validate calculated uncertainties
 - Best done experimentally
 - Repeat the measurement on another occasion; vary as much as possible
 - Use a different measurement method
 - Compare with someone else
- Internal consistency can give a false sense of security
 - Ultimate test is always to compare with other labs
 - Looking at other people's uncertainty budgets can give new ideas
- Using a range of artefacts can reveal unexpected issues
 - Helps to understand measurement system better
 - Can identify 'unknown unknowns'
- Comparisons help develop a 'gut feeling' about uncertainty
 - If calculated uncertainty 'feels too low', it often is!

Things to take away from Centre for this module National Physical Lab It's important to test / validate calculated uncer Principles apply as to NMIS! Best done experimentally Repeat the measurement on anothe sible Use a different measurement. Compare with someone Internal consist Ultime' relop a 'gut feeling' about uncertainty Compari If calcul Acertainty 'feels too low', it often is!